## MET 200 Lecture 17

 The Simple Science of Flight

## Hurricanes

 in Hawaii Hazards and Forecasting

Hurricane Neki

- Hurricane's in Hawaii
- Hurricane hazards
- Hurricane forecasting


The Simple Science of Flight


Why do birds fly? I'm not sure, but that's a different lecture.

## The Simple Science of Flight



Some quick definitions used in this lecture Velocity - distance per unit time, $\mathrm{m} / \mathrm{s}$
Acceleration - change in velocity per change in time, $\mathrm{m} / \mathrm{s}^{2}$ Force - mass times acceleration, Newton, $\mathrm{kg}^{*} \mathrm{~m} / \mathrm{s}^{2}, 1 \mathrm{~N}=102 \mathrm{gm}$ Energy (Work) - force over a distance: Joule, $\mathrm{J}=\mathrm{Nm}=\mathrm{kg}^{*} \mathrm{~m}^{2} / \mathrm{s}^{2}$ Power - energy per time, Watt $=\mathrm{J} / \mathrm{s}=\mathrm{Nm} / \mathrm{s}=$ force $\times$ speed

## Bernoulli's Principle and Lift

Bernoulli's principle states that, "In a flow where no energy is being added or taken away, the sum of its various energies is a constant: consequently where the velocity increases the pressure decreases and vice versa."


## Bernoulli's Principle and Lift



To understand flight, a good place to start is the weight a pair of wings can support. Bernoulli's principle applied to airfoils: the airspeed over the top of the wing has to be faster than that below, because the air over the top "has to rejoin" the air along the bottom, faster air means lower pressure and hence the generation of lift on the wing


Wait a Minute, What about Bernoulli!

$\qquad$

## Lift



When the angle of attack reaches $\sim 15^{\circ}$, the airflow over to top surface is disrupted causing the drag to increase a lot and the plane to drop like a brick. Pilots call this "stall."

## Bernoulli’s Principle

Bernoulli's principle evoked to explain flight is a "polite fiction." It does not provide nearly enough lift to keep a bird or an airplane aloft. In fact the air flowing over and under the wing does not rejoin as your high school teacher told you.



Force (or lift) equals the rate of change of momentum or mass flow past a wing times the change in speed.

Mass flow $=\rho V A \mathrm{~kg} / \mathrm{s}$
where $\rho=$ air density, $V=$ air velocity, and $A=$ Area of the wing
The downward motion imparted to the air flowing around a wing is proportional to the flight speed $(V)$ and the angle of attack of the wing $(\alpha)$. Thus the lift ( L ) on the wing is given by:
$L=\alpha \rho V^{2} A \mathrm{~kg} \mathrm{~m} / \mathrm{s}^{2}$ or newtons

First-Class Lift

$L=\alpha \rho V^{2} A \mathrm{~kg} \mathrm{~m} / \mathrm{s}^{2}$ or newtons
At 12 km the air density is $1 / 4$ that at sea level, you will have to fly twice as fast to obtain the same lift.
To support horizontal flight, lift = weight $(W)$. So we can write:

$$
L=W=0.3 \rho V^{2} A \text { newtons, }
$$

where the constant 0.3 is valid for long distance flight with an average angle of attack of $6^{\circ}$.

## Lift, Weight, and Cruising Speed



Wandering Albatross $\mathrm{V}=43 \mathrm{mph}$

## Lift, Weight, and Speed

If we divide both sides of Eq 1 by the wing area $A$ and replace the variable density $\rho$ by its value at sea level where birds fly, we get:

$$
W / A=0.38 \mathrm{~V}^{2}
$$

This formula tells us that the greater a bird's wing loading, the faster the bird must fly.


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## Lift, Weight, and Speed

When the weight increases by a factor of 100 , the wing loading increases by a factor of 5 , and the airspeed by a factor of more than 2.
The slope in the graph is given by:

$$
\begin{equation*}
W / A=c \times W^{1 / 3} \tag{2}
\end{equation*}
$$

which is a universally applicable scale relation whenever weights and supporting surfaces are involved.

## Natural Convergence



Evolution in nature and technology rewards good performance.





Largest flying animal known. Weighed 700 newtons ( 150 lbs ), wing area of $8 \mathrm{~m}^{2}$, soaring flight speed $15 \mathrm{~m} / \mathrm{s}(33.5 \mathrm{mph})$

## Breaking the Sound Barrier



Breaking the sound barrier is very costly, because of the large increase in aerodynamic drag: $3 x$ the drag of that below the sound barrier. Concord's fuel consumption was outrageous.

## Reducing Drag in a Dive



Reducing wing area reduces drag. Peregrin Falcons have been clocked at $242 \mathrm{mph}(390 \mathrm{kph})$.

## Increasing Drag for Landing



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Humming Birds, Bees and the Trend Line


Art of Staying Airborne


The Skater's Edge


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## Skater's Free Gearbox



The free gearbox: $100 \%$ of the work done by the large force $Z$ at the small speed $w$ is converted into the work done by the small thrust $T$ at the high forward speed $V$. To gain more speed V , simply push off harder to increase $Z$, without changing the frequency of the strokes.

## Skater's Free Gearbox



The art of skating produces a fully automatic gear. The motion of the leg generates a large sideways force $Z$, but also a forward force, thrust T. Proportional triangles show that the ratio $T / Z=w / V$. Rewriting we see that $T V=Z w$; the power propelling the skater forward equals the power generated by the skater's leg.

## Beating Wings



A bird in flapping flight faces essentially the same problem as a skater, because beating its wings too rapidly as its speed increases will cause a buildup of lactic acid in its muscles, the bird must find a way of flapping that limits the frequency of its wing strokes.


As the wing moves down, the lift force generates power. This power, the product of $L$ and $w$, is transmitted in its entirety to the propulsive effort, the product of T and V .

## Thrust vs Drag



The force balance in horizontal flight - The weight $W$ is balanced by the aerodynamic lift L , and the aerodynamic drag $D$ is overcome by the thrust $T$. Power is force times speed, so the product of $T$ and $V$ is the work that must be performed per second to maintain horizontal flight against drag. $P=T V$


Birds don't row with their wings, rather the wing is brought forward and down. To keep the wing-beat frequency down, a bird simply maintains a small angle between the wing stroke and the direction of flight, thus minimizing the loss of energy to the air..

## Gliding




In the absence of thrust, a bird or plane cannot maintain the balance of forces required for horizontal flight; it will inevitably lose altitude. When an airplane or bird descends a new balance is obtained.

## Finesse



The force and speed triangles also provide useful information on the distance that can be covered in a glide. If $U$ equals the horizontal component of the airspeed, the ratio between it and the rate of descent $w$ must be equal to the ratio of the lift $L$ to the drag $D$. $L / D=$ $\mathrm{U} / \mathrm{w}$, determines how many meters a gliding bird or plane can travel for each meter of descent.

## Gliding with Finesse



The force and speed triangles again have the same proportions. Thus, w/V = D/W, and Gw = DV. The power DV required to overcome the aerodynamic drag is supplied by the large force of gravity $G$ acting on the small downward speed w.

## Finesse

The French call the ratio of the lift $L$ to the drag $D$ of a bird or plane its finesse (F). Aeronautical engineers speak of the glide ratio when they talk about the finesse of an airplane.



## Gliding on Wind Shear



An albatross glides just above the waves for long distances without flapping their wings. How do they do this?
They extract energy from the wind shear in the MBL. Consider the balance between kinetic energy and gravitational potential energy of the bird;
$1 / 2 m v^{2}+m g z=$ constant
in differential form: $v d v=-g d z$

## or $d v / d z=-g / v$

For a gliding bird to remain airborne, the wind speed in the MBL must increase by a factor of $\mathrm{g} / \mathrm{v}$ plus drag.
A large gliding velocity $V$ is very helpful in this. And the albatross is perfectly adapted.

The Great Gliding Diagram


Madagascan Comet Moth


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## Dynamic Soaring



In dynamic soaring the albatross turns into the wind to gain height $(\sim 15 \mathrm{~m})$ and turns away from the wind to gain speed ( $\sim 25 \mathrm{~m} / \mathrm{s}$ ).

## Dynamic Soaring



Most (72\%) of the increase of wind speed within the lowest 10 m of the profile is located in a $\sim 2 \mathrm{~m}$ thick wind-shear boundary layer near the surface (shaded layer). On crossing the wind-shear layer, the bird's airspeed abruptly increases. The increase in airspeed can be used to climb up to heights of 1015 m by trading airspeed (kinetic energy) for height (potential energy)

## Powered Flight



## Power: A Hard Days Flight




Wind tunnel tests show that a bird can generate $\sim 100$ watts per kilogram of muscle mass (a human can manage only 20). The lungs of birds have air sacs behind them, so they are ventilated twice during each respiration cycle. The pectoral muscles of a bird account for about 20\% of its total mass.

## A Hard Days Flight



The tests show the parakeet 's most economical speed was~8 m/s (18 $\mathrm{mph})$. At that speed the parakeet required 0.75 watt ( 0.001 horse power) to remain airborne. At lower and higher speeds more power was needed.


To fly at constant speed a bird or a plane must develop enough thrust $T$ to overcome aerodynamic drag $D$. Power equals force times speed: $P=T V=D V$. And $D=P / V$. For our parakeet the speed at which the drag is a minimum ( $\sim 11 \mathrm{~m} / \mathrm{s}, 25 \mathrm{mph}$ ) is higher than the speed at which the power is a minimum ( $8 \mathrm{~m} / \mathrm{s}, 18 \mathrm{~m} / \mathrm{s}$ ).

## A Hard Days Flight




The flight muscles of a 35 gram parakeet weigh about 7 g , corresponding to a continuous output of about 0.7 watt, close to the minimum power in the curve above. The maximum continuous power is about twice the normal rate, or 1.4 watt, corresponding to a minimum flight speed of $5 \mathrm{~m} / \mathrm{s}$.

## How do Cars

## Match up?

Engine power plotted vs maximum speed for four makes of car.
Power required increases as the third power of the speed.
Cars have awful aerodynamic properties caused by turbulence around the wheels and in the wheel wells.



To go twice as fast requires an eightfold increase in engine power.

## For the Speed Demon



A sport plane with a Porsche engine and retractable landing gear can easily attain speeds of 250 mph ( $\sim 400 \mathrm{kph}$ )

Migration

How much food do birds need when they migrate south in the autumn?


Energy and Migration


Starling Murmuration http://vimeo.com/50014387

Radar is used in Migration Studies


## Mute Swan



A mute swan cruises at $\sim 20 \mathrm{~m} / \mathrm{s}$. It weighs $10 \mathrm{~kg}, 2 \mathrm{~kg}$ of which constitute its flight muscles. In cruising flight, the power output of these flight muscles is $\sim 100$ watts $/ \mathrm{kg}$, or about 200 watts mechanical power during migration.

## Migration



This energy is supplied by the spare fat on the bird's chest. The nutritional value of bird fat is $\sim 32 \mathrm{~J} / \mathrm{gm}$. Since a swan requires $40 \mathrm{~J} / \mathrm{m}$, it consumes 1.2 gm of fat per km . After 12 hours of cruising at $20 \mathrm{~m} / \mathrm{s}$, the swan has traveled 870 km and lost more than 1 kg of body weight. The swan will not only be exhausted, but also famished. A light snack will not suffice. Thus, it is easy to understand the importance of bird sanctuaries.

Migration


Because the conversion efficiency of nutrient energy is only about $25 \%$, the swan needs 800 watts of nutrient energy. At a speed of $20 \mathrm{~m} / \mathrm{s}$ this corresponds to an energy consumption of $40 \mathrm{~J} / \mathrm{m}$.

## The Amazing Bar-Tailed Godwit



Bar-Tailed Godwits are large wading birds that cross the entire Pacific Ocean without refueling.

## Bar-Tailed Godwit Migration



Do They Violate the Laws of Physics?


Upon their arrival in New Zealand, their weight has dropped to 220 gm . The metabolic energy consumed is about 9000 kilojoules. With a conversion efficiency of $25 \%$, this becomes $\sim 2,300$ kilojoules mechanical. On average during the trip their lift to drag ratio (finesse) is 14 and their drag is 0.26 newton, resulting in a flight range of $8,800 \mathrm{~km}-2,200 \mathrm{~km}$ short of their goal of $11,000 \mathrm{~km}$. How do they do it?

## Bar-Tailed Godwit Migration



Their takeoff weight is 500 g , wingspan 0.73 m , wing area is $0.57 \mathrm{~m}^{2}$, leading to a cruising speed of $15 \mathrm{~m} / \mathrm{s}$. Their flight muscle mass is 70 gm at takeoff, providing 7 watts of power. To overcome their drag, they need about 6 watts, so they are cutting it close.


Elementary meteorology, dear Watson

1. They take off with a strong tail wind ( +1700 km )
2. They climb high enough to profit from counter trades in SH (+ 1000 km )
3. Their metabolic efficiency may be closer to $30 \%$ without steroids (+1500 km)

Now they arrive with 1000 km to spare.

## Questions?



Acknowledgement: much of the material in this talk is from:
The Simple Science of Flight by Henk Tenekes

Questions?


