



#### **Definitions**

• <u>system</u> - a collection of matter in an identifiable place and condition. A system can contain more than one *chemical* component and more than one physiochemical phase.

• A <u>component</u> is a chemical entity (e.g.,  $H_2O$ ) that can be used to describe compositional variation in a system.

Normally, we choose the minimum number of components (C) to describe the system: C = n - r, where n is the number of chemical species and r is the number of reactions that can occur between these species. A <u>component need</u> <u>not physically exist</u> in a system (e.g., plagioclase can be described as a solid-solution mixture of albite and anorthite components, but neither exists in a plagioclase grain of intermediate composition, like labradorite or andesine).

• A phase is a physical form of that chemical

e.g., for H<sub>2</sub>O: ice, water vapor, liquid water for SiO<sub>2</sub> quartz, chert, cristobalite.







## **Chemical Thermodynamics**

 Please refresh your memory on: enthalpy (H) entropy (S)
 Gibbs function (G) and their relationships to measures of chemical equilibrium (and chemical equilibrium constants, K). for instance, the last slide of last lecture, inserted after this slide for convenience

In all cases the standard state condition (annotated by " $^{\circ}$ " next to the variable) is for STP (298.15 $^{\circ}$ K = 25 $^{\circ}$ C, 1 atm)



Some Thermodynamic Quantities and Relationships
The laws of thermodynamics and the mathematical relationships that derive from them describe infinitesimal changes to system variables ("variables of state") using differential calculus – see the White text for these derivations.
In this class we will only "break down" the energetics of reactions part of the way.
You will not have to derive thermodynamic expressions from first principles and partial differential equations.
The "finite" change versions of various equations will be sufficient (e.g., ΔH, ΔG) for our applications.

Variables such as G, H and S are not measurable as absolute values. Instead, G, H and S are compared to reference materials in the standard state for which arbitrary values (typically 0) are defined.

The variable (G, H or S) is then defined as a  $\Delta$  (change) relative to that (i.e.,  $\Delta$ G,  $\Delta$ H or  $\Delta$ S).

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# <u>Enthalpy – H</u>

Enthalpy is a measure of energy in the form of heat (which itself is a measure of molecular vibration or motion).

Enthalpy is important for understanding the energy consumed or released in changes of state of a system.

#### The relationships between

heat (Q) and work (W = -P $\Delta$ V) to internal energy (U, e.g.,  $\Delta$ U = Q + W) and enthalpy (H, e.g., H = U + PV)

### are details we are going to skip over here (see equations in the reading if you're interested in the details).

### Enthalpy – H

 $\Delta H = \Delta U + V\Delta P + P\Delta V, \text{ or } \Delta Q + \Delta W + V\Delta P + P\Delta V$ which reduces to  $\Delta H = \Delta Q + V\Delta P$ It is therefore useful to remember that at **constant pressure** :

 $\Delta H = Q$ 

(the Enthalpy change of a process is the heat gained or lost in the process)

 $\Delta H = C_p \Delta T \qquad (where C_p = heat capacity)$ 

(the Enthalpy change of a process is the heat capacity times the temperature change)

and...

 $\Delta H = T\Delta S + V\Delta P$  at **constant temperature** (the Enthalpy change of a process is relates to changes in entropy, which we define momentarily, and pressure)





<u>Enthalpy – H</u>	1. "Bond Heat"			
If two reactions can be mathematically combined to make a third, we can also combine their $\Delta H_f^{\circ}$ to calculate $\Delta H_f^{\circ}$ of the new reaction.				
For example, we might find these two reactions in a table: 1. C (graphite) + $O_2(g) \leftrightarrow CO_2 \qquad \Delta H_f^\circ = 94.051 \text{ kcal/mol}$ 2. C (diamond) + $O_2(g) \leftrightarrow CO_2 \qquad \Delta H_f^\circ = 94.504 \text{ kcal/mol}$				
if we reverse the order of equation 2 and change the sign of $\Delta H_{f}^{\circ}$ , we can add the two to get C (graphite) $\leftrightarrow$ C (diamond)				
$\Delta H_{f^{\circ}} = (94.051 - 94.504) k$ $\Delta H_{f^{\circ}} = -0.453 \text{ kcal/mol}$	cal/mol = -1.897 kJ/mol			
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Entropy - S				
Entropy is a measure of system disorder.				
In general, systems tend to evolve toward less ordered conditions, reflected in the amount of heat absorbed by a system from its surroundings during any physiochemical change at a given temperature.				
$\Delta S = Q_r/T$ in other words, $Q_r = T\Delta S$				
also, at constant P, $\Delta S = C_p / \Delta T$ (where $C_p$ = heat capacity)				
The standard state for any compound S° is determined relative to S° of H <sup>+</sup> = 0 at STP.				
The calculation of $\Delta S^{\circ}_{reaction}$ is the same as that for H:				
$\Delta S^{\circ}_{reaction} = \Sigma \Delta S^{\circ}_{f}$ (products)- Σ $\Delta S^{\circ}_{f}$ (reactants)				
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<b>"Free Energy", or the Gibbs Function – G</b> Let's solve a problem using the relationship of G and K What is $K_{eq}$ for the precipitation reaction of the mineral malachite from water?				
2Cu <sup>2+</sup> (aq) + "copper 2+ cation"	CO <sub>3</sub> <sup>2-</sup> (aq) + "carbonate anion"	2 OH-(aq) ↔ Cu <sub>2</sub> (OH "hydroxyl "malachin anion"	H) <sub>2</sub> CO <sub>3</sub> (s) <sup>te"</sup>	
First, notice how the equation is balanced:				
material:	Cu	2	2	
	CO <sub>3</sub>	1	1	
charge.	OH	2 A (2x2)	2	
charge.	CO₂	-2		
	OH	-2 (-1x2)		
	Cu <sub>2</sub> (OH) <sub>2</sub> CO <sub>3</sub>		0	
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## "Free Energy", or the Gibbs Function – G

Next, get  $\Delta G^{\circ}_{reaction} = \Sigma \Delta G_{f}^{\circ}(products) - \Sigma \Delta G_{f}^{\circ}(reactants)$  using values for  $\Delta G_{f}^{\circ}$  from a compilation of thermodynamic data.

A word on units:

Always watch units when solving problems using thermodynamic equations. •R is the Universal Gas Constant (8.314 J = 0.08206

•L-atm = 82.06 cm<sup>3</sup>-atm = 1.987 calories all per mol °K).

•R should be in the same system of units as the thermodynamic data you are using Some books give R in non-standard units (cm3-atm/mol-oK) or (cal/mol-oK). Others use

the SI units: use J/mol-ºK and J/mol, respectively.

2Cu<sup>2+</sup>(aq) +  $CO_3^2$ -(aq) + 2 OH-(aq)  $\leftrightarrow$   $Cu_2(OH)_2CO_3$  (s)

ΔG°<sub>reaction</sub>=-216.44-(2·15.50+ 2·-37.60 -126.22) kcal/mol

 $\Delta G^{\circ}_{reaction}$ =-46.02kcal/mol = -46,020 cal/mol

From  $\Delta G^{\circ}$  = -RT lnK, we get  $\Delta G^{\circ}/(RT)$  = -lnK

 $-46,020/(298.15\cdot1.987) = -InK$  K =  $e^{46,020/(298.15\cdot1.987)}$ 

K= 5.45 x 10<sup>33</sup> or about 10<sup>33.7</sup>